

## **Differential Equations in introductory physics.**

The purpose of the following is to use specific physics mechanics problems to motivate a consideration of the role and solution of 2<sup>nd</sup> order, linear differential equations with constant coefficients. Of course the acceleration “a” in Newton’s 2<sup>nd</sup> law immediately leads to such a differential equation.

### **Problem: Chain falling off a pulley. 2<sup>nd</sup> order differential equation with constant coefficients.**

Consider a chain of mass  $M$ , length  $L$  and density  $\rho=M/L$ . The chain is hung over an idealized pulley (frictionless, no moment of inertia, and negligible radius). Initially (at  $t=0$ ) the chain is at rest and its long side hangs a distance  $x_0$  lower than the unstable equilibrium distance  $L/2$  below the pulley. Find the expression for the distance the  $x(t)$  that the long end of the chain moves down as a function of time.

For solution see:

<http://www.physics.rutgers.edu/~croft/Diff-Eq-in%20-Phys/chain-pulley-diffeq.pdf>

### **Problem: Spring, simple harmonic motion. 2<sup>nd</sup> order differential equation with constant coefficients.**

Consider mass  $M$ , attached to a spring with spring constant  $k$ . Initially (at  $t=0$ ) the mass is at rest and is displaced to its maximum amplitude  $x_0$  from the stable equilibrium position  $x=0$ . Find the expression for the position of the mass,  $x(t)$  as a function of time.

For solution see: <http://www.physics.rutgers.edu/~croft/Diff-Eq-in%20-Phys/SHM-diffeq.pdf>

Actually before visiting the above review the discussion of complex variables at the link

<http://www.physics.rutgers.edu/~croft/Diff-Eq-in%20-Phys/z-complex-var-impedance.pdf>

Selected additional discussion of differential equations in introductory physics is at:

<http://www.physics.rutgers.edu/~croft/Diff-Eq-in%20-Phys/z-differentialequations.pdf>